# Problems associated with analysis and interpretation of small molecule/macromolecule binding data

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In the analysis of binding data, arbitrary transformations such as the Scatchard plot, may give misleading estimates of the binding parameters. The statistically correct approach is to determine values of K and n by non-linear regression of the actual dependent variable against the actual independent variable. In the case of the spectrophotometric titration method the dependent variable is the absorbance and the independent variable is the composition of the drug/macromolecule mixture. The method relies on an accurate estimate of the extinction coefficient of the bound drug and this is best treated as a parameter to be estimated in the regression analysis. In testing models by data fits alone it is emphasized that whilst a model may be rejected if it does not fit the data, a good fit does not ensure uniqueness and confirmatory, independent evidence must be sought.

For an interaction of the following type:

Drug + Macromolecule  $\rightleftharpoons$  Drug/Macromolecule the concentration of the bound drug may be related to the concentration of unbound drug by the Law of Mass Action:

$$\mathbf{K} = \frac{\mathbf{r}}{\mathbf{c}(\mathbf{n} \cdot \mathbf{r})} \qquad \dots \qquad (1)$$

where K is the association (or affinity) constant; r is the concentration of bound drug/concentration of macromolecule; c is the concentration of unbound drug; n is the number of binding sites for drug per macromolecule.

To determine K and n, a study of the degree of binding at various ratios of total drug to macromolecule is performed. The total concentration of drug (bound + unbound) and concentration of macromolecule are known for each sample of the drug/macromolecule mixture and it is usual to determine the concentration of unbound drug (c). The value r can then be calculated. In order to calculate K and n, equation (1) is usually rearranged to a linear form, most commonly using the method of Scatchard (Scatchard, 1949):

$$\mathbf{r/c} = -\mathbf{Kr} + \mathbf{Kn} \qquad \dots \qquad (2)$$

The Scatchard plot of r/c vs r gives a line of slope -Kand an intercept Kn on the ordinate. A linear regression analysis is then performed to determine the slope of the line and the intercept. The advantage of a plot of this nature is that it gives a visual representation of the results. However, curvature is often found since the plot will only be linear if there is a single

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type of non-interacting site. Curvature in a Scatchard plot is difficult to interpret and any interpretation is dependent on the method of analysis used (Weder, Schildknecht & others, 1974). A second and major objection to the Scatchard plot is that even if a straight line is found, the method is still inappropriate since the conditions for use of linear regression analysis are not fulfilled (Draper & Smith, 1966). If y is regressed against x then the error in the variable x should be much less than that in y and the error about y should be normally distributed and independent of x and y. Clearly it is statistically incorrect to use a linear regression on the Scatchard plot of r/c vs r since r and c are both functions of the same variable, namely bound drug concentration. This criticism also applies to the plot of c/r vs c (Klotz & Urquhart, 1949) and to the double reciprocal plot (1/r vs 1/c)commonly employed in enzyme kinetics (Lineweaver & Burk, 1934). The limitations of linearization of binding data have in fact long been recognized in the field of enzyme kinetics (Wilkinson, 1961) where for example the non-parametric direct linear plot (Cornish-Bowden & Eisenthal, 1974) has been shown to give more reliable parameter estimates than linear transformations of the data (Atkins & Nimmo, 1975). Similarly, criticisms can also be made of the nonlinear double log plot (log r vs log c: Thompson & Klotz, 1971) and semi-log plot (r vs log c: Bjerrum, 1941) and of the step-wise model (Fletcher, Ashbrook & Spector, 1973; Klotz & Hunston, 1975). The correct way to analyse binding data is to derive the constants K and n directly from the binding isotherm. However, although methods are available for non-linear regression of binding isotherms (Perrin, Vallner & Wold, 1974; Madsen & Robertson, 1974)

the Scatchard plot and other similar transformations are still commonly used.

In this paper we examine some of the errors involved in using the Scatchard plot and advocate the use of a non-linear regression method. The interaction of daunomycin with DNA has been chosen as the example since the nature of this interaction can be predicted with confidence (Di Marco & Arcamone, 1975). At low ratios of daunomycin to DNA, the drug intercalates into the helix (Pigram, Fuller & Hamilton, 1972) then, as the ratio of drug to DNA increases, additional drug molecules bind to the exterior of the helix (Zunino, Gambetta & others, 1972). We have attempted to negate this latter mode of binding by carrying out the studies in buffer containing 0.3 M sodium chloride. Under these conditions there should be a single intercalative mode of binding (Zunino, 1971).

### MATERIALS AND METHODS

A spectrophotometric titration was performed by sequential addition of a solution of DNA in 0.008 M tris-Cl, 0.3 M NaCl buffer at pH 7.0 to  $3 \times 3 \text{ ml}$ aliquots of a solution of daunomycin hydrochloride  $(5.833 \times 10^{-5} \text{ M})$  in the same buffer, at room temperature (20°). After allowing time for equilibration the absorbance was measured at 480 nm (the  $\lambda$ max of unbound daunomycin) after each addition of DNA. The apparent extinction was calculated allowing for the change in volume. The DNA solution used was  $2.538 \times 10^{-3}$  M Sigma Type I calf thymus DNA, assayed at 260 nm using the figure  $\epsilon(P)_{260} = 6600$ . The protocol for the sequential addition of this DNA solution was as follows: 2 aliquots each of 40  $\mu$ l, 16 aliquots each of 20  $\mu$ l, 7 aliquots each of  $100 \,\mu$ l; giving a total addition of 1.10 ml to each 3 ml sample of drug solution, in 25 aliquots.

#### RESULTS

The data have been evaluated by the Scatchard plot, by non-linear regression of r vs c and by non-linear regression of the fraction of drug bound vs the cumulative volume of DNA added. It will be shown that only the latter method of interpretation is valid.

### Scatchard plot

In order to evaluate data by the Scatchard plot, r/c and r must be calculated. On binding to DNA daunomycin shows a bathochromic shift and a decrease in extinction, and an isosbestic point is observed (Di Marco & Arcamone, 1975). The fraction of drug bound after each addition of DNA can

therefore be calculated using equation (3) (Peacocke & Skerret, 1956).

$$\alpha = \frac{\epsilon_{\rm f} - \epsilon_{\rm obs}}{\epsilon_{\rm f} - \epsilon_{\rm b}} \qquad \cdots \qquad (3)$$

where  $\epsilon_1$  is the extinction of the unbound (free) drug,  $\epsilon_{obs}$  is the apparent extinction and  $\epsilon_b$  is the extincton of the drug when bound to DNA. Knowing  $\alpha$ , r/c and r can now be calculated since c is equal to  $(1-\alpha)Ct$ and r is equal to  $\alpha Ct/DNAP$ , where Ct is the total concentration of drug and DNAP is the concentration of DNA expressed in terms of phosphorus. The parameters  $K_1$  and  $n_1$  were calculated by linear regression of the initial linear segment of the Scatchard plot of r/c vs r. These values of  $K_1$  and  $n_1$  are given in Table 1.

It is evident that there must be a reliable estimate of  $\epsilon_{\rm b}$ , and several methods are available (Bontemps & Fredericq, 1974). In the present study  $\epsilon_{\rm b}$  was found from a plot of  $\epsilon_{\rm obs}$  vs DNAP/Ct (Double & Brown, 1975). As DNAP/Ct increases  $\epsilon_{\rm obs}$  decreases until the drug is fully bound; the plot then plateaus and  $\epsilon_{\rm b}$  was found to be  $6 \cdot 172 \times 10^3$  by linear regression in this region. By averaging the initial values for the three samples (containing no DNA)  $\epsilon_{\rm f}$  was found to be 9.991  $\times 10^3$ .

### Non-linear regression of r vs c

The values of r and c were next fitted to the equation for a one site model:

$$\mathbf{r} = \frac{\mathbf{K}\mathbf{c}\mathbf{n}}{1 + \mathbf{K}\mathbf{c}} \qquad \dots \qquad (4)$$

using the non-linear regression program NONLIN (Metzler, Elfringe & McEwan, 1974) with r treated as the dependent variable and c as the independent variable. The value of K (Table 1) estimated by this procedure is lower than that predicted by the Scatchard plot since, unlike the Scatchard plot, all the points have been fitted in this non-linear treatment. To allow for the curvature in the Scatchard plot, equation (4) can be modified to accommodate the possibility of a second site as shown in equation (5):

$$\mathbf{r} = \frac{\mathbf{K}_{1}\mathbf{n}_{1}\mathbf{c}}{1 + \mathbf{K}_{1}\mathbf{c}} + \frac{\mathbf{K}_{2}\mathbf{n}_{2}\mathbf{c}}{1 + \mathbf{K}_{2}\mathbf{c}} \qquad .. \tag{5}$$

The data were fitted to equation (5) using the NONLIN program and a closer agreement was noted between the values of the parameters  $K_1$  and  $n_1$  determined in this manner and those derived from the Scatchard plot (Table 1). However, the plot of

residuals (calculated r — observed r vs calculated r) shows a systematic trend (Fig. 1a), undoubtedly due to the fact that both r and c are subject to error. In order to correct this, it is necessary to regress the data against the true independent variable.

### **Regression** of fraction bound $(\alpha)$ vs cumulative volume of DNA added (x)

If  $x_1$  represents the volume of the i th aliquot of DNA solution added to the drug solution then the cumulative volume  $\sum x_1$  is the true independent variable. Although this variable is subject to some error, this is much less than the error incurred in  $\alpha$  which is therefore treated as the dependent variable. Substitution of  $\alpha$ Ct/DNAP for r and (1- $\alpha$ )Ct for c in the equation for a one-site model, equation (4), yields:

$$\frac{\alpha}{DNAP} = \frac{nK(1-\alpha)}{1 + K(1-\alpha)Ct}$$
$$\alpha = \frac{a - \sqrt{a^2 - 4nK^2CtDNAP}}{2KCt}$$

where  $Ct = (C_D V)/(V + x)$ ,  $DNAP = (C_A x)/(V + x)$ ; a = (1 + KCt + nKDNAP)

**x** is the cumulative volume of DNA added and the constants  $C_D$ , V and  $C_A$  are the initial concentration of drug solution, the initial volume of drug solution and the concentration of master DNA solution respectively. A similar treatment for a two site model gives a cubic equation in  $\alpha$  which also has a closed analytical solution.

The data were fitted to both the one site and the two site models (Table 1), the two site model giving

the best fit to the data as expected. Examination of the residual plots (Fig. 1b) shows a lessening of the systematic trend seen for the regression of r vs c (Fig. 1a) but it is evident that there are three distinct groups, parallel to the residual axis. This can only be due to combining the data points from all three samples of daunomycin solution to obtain a common  $\epsilon_f$  and  $\epsilon_b$  which were then used to calculate the values of  $\alpha$ . Consequently an individual  $\epsilon_{f}$  and  $\epsilon_{h}$  was determined for each sample of daunomycin solution and the values of  $\alpha$  recalculated using the appropriate values of  $\epsilon_f$  and  $\epsilon_b$ . The three data sets were fitted simultaneously to the two site model, the results showing a distinct improvement (Table 1). This underlines the value of analysis of residuals in regression analysis. In all subsequent analyses the cells were treated separately in this manner.

Comparison of the  $\alpha$  vs x and r vs c regression methods To assess the effect on the parameter estimates of transformation of the data, a perfect set of data was generated for  $\alpha$  and x with a normally distributed random noise added to  $\alpha$ . The parameters n and K for a two site model were then determined by the  $\alpha$  vs x method and, after transformation of the data, by the r vs c method (Table 2). Both methods gave broadly similar results for the data with least scatter ( $\sigma = 0.02$ ), but as the scatter was increased ( $\sigma =$ 0.04) the parameter estimates from the r vs c method were found to diverge dramatically from the theoretical values. Also, the residual plots for the r vs c regression (Fig. 2a) show the same systematic trend seen when regression of r vs c was used to analyse the

Table 1. Binding parameters for the titration of daunomycin with DNA.

Method of evaluation	K1 × 10-6	n,	$\omega \times 10^{-3}$	$K_{a} \times 10^{-3}$	n.	r	r <sup>2</sup>	$SSE \times 10^{2}$
Scatchard plot	1.734	0.153				0·774	_	
r vs c (1 site)	0·786 (0·424)*	0·156 (0·002)	_			<b>0</b> ·899	<b>0</b> ·804	1.46
r vs c (2 site)	1·605 (0·278)	0·116 (0·005)		56.504 (19·042)	0·060 (0·013)	<b>0</b> ·914	<b>0</b> ·836	1.23
α vs x (1 site)	0·627 (0·040)	0·157 (0·001)		_		0.998	0.995	2.63
a vs x (2 site)	0·855 (0·100)	0·146 (0·001)	_	0·431 (2·580)	0·773 (4·600)	<b>0</b> ·998	0.996	2.44
α vs x (2 site) (cells treated separately)	1·329 (0·124)	0·143 (0·003)		0·611 (7·643)	0·749 (9·060)	1.000	1.000	0.24
Non-cooperative binding model (cells treated separately)	6·482 (1·690)	0·171 (0·003)	4·253 (0·570)	_		1.000	1.000	0-27

(6)

Values in parentheses are standard deviations.

<sup>†</sup> Sum of squared deviations due to error.



FIG. 1. Residuals plot for non-linear regression of (a) r vs c. (b)  $\alpha$  vs x using the two site model. Ordinate: Residuals. Abscissa: Y<sub>calc</sub>.

 Table 2. Non-linear regression analysis of perfect data with scatter.

	Set	σ ==	0.02	$\sigma = 0.04$		
	values	rvsc	α <i>vs</i> x	r vs c	αvs x	
K <sub>1</sub> × 10 <sup>-6</sup>	1	1.111	0.8555	99.98	0.6647	
		(0.2137)	(0.1518)	(264-48)	(0.2971)	
n.	0.2	0.186	0.209	0.090	0.236	
		(0.017)	(0.015)	(0.014)	(0.052)	
K. × 10-4	1	1.0527	0.7238	3.390	0.5978	
	-	(0.4896)	(0.4650)	(1.4892)	(1.6801)	
n.	0-8	0.842	0.986	0.611	1.000	
		(0.234)	(0.454)	(0.122)	(2.111)	
•		0.000	0.999	0.933	0.996	
**		0.980	0.999	0.854	0.991	
**N1 V 301		1.97	0.55	9.20	1.83	

\* Sum of squared deviations due to error.

experimental data (Fig. 1a), whereas the residual plot for regression of  $\alpha$  vs x shows random scatter (Fig. 2b). This confirms that transformation from  $\alpha$  vs x variables to r vs c variables before analysis will give erroneous results. Most experimental data will probably have a variance greater than that in the second set of data where  $\sigma = 0.04$ .

### A non-cooperative binding model

Since the data fit a two site model when  $\alpha$  is regressed against x, there is now a temptation to conclude that there are two types of binding site for daunomycin on DNA under the conditions of the assay. Indeed, it is known that there are two possible modes of binding of daunomycin to DNA, intercalation and external



FIG. 2. Residuals plot for non-linear regression of (a) r vs c. (b)  $\alpha$  vs x using the two site model and perfect data with scatter ( $\sigma = 0.04$ ). Ordinate: Residuals, Abscissa: Y<sub>cale</sub>.

binding (Di Marco & Arcamone, 1975), however, only the former mode of binding should occur in the buffer containing 0.3 M sodium chloride. It is possible that as daunomycin intercalates into the helix, the binding of subsequent molecules becomes increasingly hindered due to a non-cooperative binding process. In fact a 'nearest neighbour exclusion' model has been proposed for intercalating drugs, the intercalation only being allowed at alternate base pairs (Crothers, 1971). To investigate this model, an analysis was performed in which the parameter K was varied by inclusion of an interaction parameter  $\omega$  in the manner of the Deybe-Huckel theory in solution kinetics (Chambron, Daune & Sadron, 1966). The resulting equation is

$$\mathbf{r} = \frac{\mathbf{K} \mathbf{e}^{-2\omega r/n\mathbf{RT}} \mathbf{cn}}{1 + \mathbf{K} \mathbf{e}^{-2\omega r/n\mathbf{RT}} \mathbf{c}} \qquad \dots \qquad (7)$$

where R and T are the gas constants and absolute temperature respectively. After substituting  $\alpha$  and x for r and c, equation (7) can be arranged to a form  $f(\alpha_1, x) = 0$ .

It is not possible to express  $\alpha$  in terms of x in a closed analytical fashion and so a numerical method must be used. The simplest method is the Newton-Raphson method which requires an initial estimate of  $\alpha$  ( $\alpha_0$ ) which is updated by the following means:

$$\alpha_1 = \alpha_0 - \frac{f(\alpha_1, x)}{\alpha f / \sigma \alpha}$$

The new (and hopefully improved) estimate of  $\alpha$  ( $\alpha_1$ ) is used as a new input and the process repeated until self-consistency is obtained to the required degree of accuracy. Although this method sometimes runs into convergence problems we experienced no such difficulty here. The parameters obtained are included in Table 1. To test for significance between the various models, an analysis of variance was performed (Table 3) on the error sum of squares of the one site  $(\alpha vs x)$  the two site  $(\alpha vs x)$  and the non-cooperative hinding model (one site model plus interaction), assuming they are nested (Boxenbaum, Riegelman & Elashoff, 1974). The analysis is not strictly correct as the non-cooperative binding model is not a subset of the two site model, nevertheless the analysis does provide a basis for comparison. The fit to the two site model is significantly better than the fit to the non-cooperative binding model (one site model plus interaction) which is significantly better than the one site model (P < 0.05).

## Non-linear regression of absorbance vs cumulative volume of DNA added (x) in which $\epsilon_{\rm b}$ for each cell is treated as a parameter to be estimated

Non-linear regression of  $\alpha$  vs x using a two site model gives the best fit to the data but there is one further point to consider, namely that  $\alpha$  is a function of both the absorbance and the 'constant'  $\epsilon_b$ . One major drawback of the spectroscopic titration method of analysing drug binding is that the data evaluation is highly dependent on the value used for  $\epsilon_b$  (Bontemps & Fredericq, 1974). To estimate the influence of  $\epsilon_b$  on the binding parameters the data were fitted to the one site and the two site models with  $\epsilon_b$  to be determined as a parameter (Table 4). Using the one site model there was a strong correlation between  $\epsilon_b$  and K and this was reflected in the lowering of the value of K when the regression was repeated omitting the 18

Table 3. Analysis of variance of the one site ( $\alpha$  vs x), two site ( $\alpha$  vs x) and non-cooperative binding models<sup>\*</sup>.

Model 1-Site	SSE 0·00671	df† 73	F‡ 62:5 (1-site
2-Site	0.00243	71	vs 2-site) 8.5 (1-site +
No.			interaction vs 2-site)
Binding (1-site + interaction)	0.00272	72	
	0.00472	. 2	

\* Boxenbaum & others (1974).

Number of degrees of freedom.

F(5%; 1, 70) = 3.98; F(5%; 2, 70) = 3.13.

points at highest concentrations of DNA. In the two site model the interaction between  $K_1$  and  $\epsilon_b$  was lessened mainly due to the fact that the two site model fits the data better than the one site model and hence the additional parameters ( $\epsilon_{b_1}, \epsilon_{b_2}$  and  $\epsilon_{b_3}$ ) do little to improve the fit. The residual plot for this two site model showed a completely random scatter, and this method gave the optimum fit to the data (Table 4). It must be emphasized that in using this method (and indeed any other method) to evaluate data from spectroscopic titrations, enough data must be obtained at sufficiently high ratios of macromolecule to drug to give unbiased estimates of  $\epsilon_b$ .

### DISCUSSION

There are a number of points which must be considered when analysing data from binding studies: 1. Transformation of binding data before analysis, such as in the Scatchard method, is statistically incorrect. The errors in the dependent (r/c) and independent variable (r) are highly correlated.

2. It is important to examine the experimental method to identify the true dependent and independent variables. The parameter estimates should be obtained from the regression of the actual dependent variable against the actual independent variable. The errors involved in using the incorrect variables are clearly seen by comparing the results from regressing r against c and  $\alpha$  against x for the same set of data (Table 2).

3. Data fitting alone cannot be used to gain information about the number of different types of binding site and their nature. If a particular model does not fit the data then it can be rejected; if, however, the

Table 4. Estimation of  $K_1$ ,  $n_1$ ,  $K_2$  and  $n_2$  with  $\epsilon_b$  fixed and as a parameter ( $\alpha$  vs x).

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	ε <sub>b</sub> estimated One site model	graphically* Two site model	ε <sub>b</sub> entered a One site model	s a parameter Two site model
$z_{b1}  imes 10^{-a}$	6.133	6.133	6.014	6.134
$z_{b2} \times 10^{-3}$	6.267	6.267	6.159	6·280
$z_{\rm bs}  imes 10^{-s}$	6.117	6.117	6·034	6.154
$K_1 \times 10^{-6}$	0.799	1.329	0.490	2.358
11	0.157	0.143	0.158	0.129
$K_{a} \times 10^{-3}$	(0.001)	0.003 0.611 (7.643)	(0.001)	(0.006) 36.097 (16.719)
12	—	0.749	—	0.052
-2	0·999 0·999	1.000	1.000	1.000
$SSE \times 10^3$	6.71	2.43	0.14	0.06

\*  $\varepsilon_b$  was determined for each of the samples of daunomycin hydrochloride from a plot of DNAP/Ct vs  $\varepsilon_{0bs}$  and linear regression of the final plateau region where drug is fully bound. The subscripts refer to the individual samples.

model does fit the data then it cannot be regarded as a unique solution. This point has not always been appreciated despite the fact that it has often been emphasised (for example Riggs, 1963; Berman, 1963) that the apparent suitability of one mathematical model over another, does not imply that the preferred model is descriptive of the binding system. The data obtained in this study can be described by a one site model with a non-cooperative interaction and if this model had been used as the sole model then it may have been concluded that daunomycin intercalates into DNA in a non-cooperative manner. In fact a two site model gives a significantly better fit to the data (Table 3). Further independent experimental results would be needed to confirm that the two site model is in fact correct.

Although estimation of the binding of a drug to DNA by spectrophotometric titration has been chosen as the example, the above conclusions are relevant to all studies of small molecule/macromolecule binding interactions including enzyme kinetics and the investigation of pharmacological response. In the spectroscopic titration method absorbance and cumulative volume added are the dependent and independent variables respectively and care must be

taken to ensure the titration is continued until drug is fully bound. In equilibrium dialysis, perhaps the most common method of analysing drug binding, a choice of dependent variable has to be made since both total drug and free drug are assayed. For highly bound drugs the total drug concentration is usually more precisely determined and so would be considered to be the independent variable: this is a rational choice since the unbound drug concentration depends on the total concentration of drug. The unbound concentration can then be regarded as the dependent variable. In analysis of binding data, the parameters K and n only have significance within the chosen model. It is therefore fallacious to imply that there are two distinct binding sites if the data will fit a two site model unless there is strong corroborative evidence from independent studies. The values of K and n can only serve to compare drugs within the context of a chosen model, all the binding studies having been conducted in an identical manner. Finally we would point out that the Scatchard plot, although statistically incorrect, is still useful both as a means of graphical representation of the data and for providing parameter estimates for the input to a non-linear regression program.

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